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| 5        | Protein homeostasis from diffusion-dependent control of protein   |
| 6        | synthesis and degradation   |
| 7        |   |
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#### 2

#### 21 Summary

22 It has been proposed that the concentration of proteins in the cytoplasm maximizes the speed of 23 important biochemical reactions. Here we have used the Xenopus extract system, which can be 24 diluted or concentrated to yield a range of cytoplasmic protein concentrations, to test the effect of 25 cytoplasmic concentration on mRNA translation and protein degradation. We found that protein 26 synthesis rates are maximal in ~1x cytoplasm, whereas protein degradation continues to rise to 27 an optimal concentration of  $\sim 1.8x$ . This can be attributed to the greater sensitivity of translation 28 to cytoplasmic viscosity, perhaps because it involves unusually large macromolecular complexes 29 like polyribosomes. The different concentration optima sets up a negative feedback homeostatic 30 system, where increasing the cytoplasmic protein concentration above the 1x physiological level 31 increases the viscosity of the cytoplasm, which selectively inhibits translation and drives the 32 system back toward the 1x set point.

#### 33 Keywords

34 Cytoplasmic concentration, protein homeostasis, diffusion control, maximal speed conjecture,

35 protein synthesis and degradation, viscosity, molecular crowding, *Xenopus* egg extract

#### 36 Introduction

37 The cytoplasm is crowded with macromolecules, with proteins being the most abundant class. In

total, proteins constitute about 82% of the dry mass of a mammalian cell (Oh et al., 2022) and

39 about 55% of an *E. coli* cell (Milo et al., 2009), and the cytoplasmic concentration of protein

40 ranges from about ~75 mg/mL in mammalian cell lines (Liu et al., 2022) and *Xenopus* egg

41 extracts (Green, 2009; Murray, 1991) to 200-320 mg/mL in *E. coli* (Elowitz et al., 1999;

42 Zimmerman and Trach, 1991). Assuming an average protein density of 1.35 g/mL, this means

43 that the volume fraction of a cell occupied by protein is  $\sim 6\%$  to 25%, and the macromolecular

44 excluded volume is higher still. Although protein concentration transiently decreases during

45 mitosis (Son et al., 2015; Zlotek-Zlotkiewicz et al., 2015), for a given cell type, the concentration

46 of macromolecules in the cytoplasm is tightly regulated and remarkably constant (Delarue et al.,

47 2018; Liu et al., 2022; Neurohr and Amon, 2020; Oh et al., 2022).

48 This brings up two basic questions: why is the cytoplasmic protein concentration as high as it is,

49 and no higher, and what mechanisms set and maintain this concentration? It has been conjectured

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50 that the normal cellular protein concentration maximizes the rates of important biochemical 51 reactions, with there being a trade-off between the effects of concentration on enzyme-substrate 52 proximity and viscosity (Dill et al., 2011). This conjecture assumes that these critical reactions 53 are sensitive to the viscosity of the medium because the collision frequency of their reactants 54 depends upon viscosity. Note, however, that decades of in vitro work has indicated that almost 55 all enzymes are reaction-limited, not diffusion-limited (Bar-Even et al., 2011), so that changes in 56 diffusion might be expected to have minimal effect on the rates of most enzyme reactions. That 57 said, there are examples of protein-mediated processes that are markedly inhibited by increased 58 viscosity (Alric et al., 2022; Drenckhahn and Pollard, 1986; Molines et al., 2022; Tan et al., 59 2013), and the simplest explanation for this is that they are diffusion controlled. Thus, the 60 maximal speed conjecture remains an intriguing possibility.

61 Here we set out to directly test the conjecture experimentally. We chose to use the *Xenopus* egg 62 extract system, an undiluted cell-free living cytoplasm, for these studies because they allow easy, 63 direct manipulation of the concentration of cytoplasmic macromolecules. Although Xenopus 64 extracts are an in vitro system, they carry out the complex biological functions of an intact 65 *Xenopus* egg or embryo remarkably faithfully. For example, extracts can self-organize into sheets of cell-like structures whose overall architecture closely resembles that of embryonic 66 67 blastomeres (Cheng and Ferrell, 2019; Gires et al., 2023; Mitchison and Field, 2021). If supplied 68 with sperm chromatin, extracts can organize a functional nucleus and carry out DNA replication. 69 Indeed, extracts can perform full cell cycles, complete with replication, mitosis, and reductive 70 division of the cell-like cytoplasmic structures (Afanzar et al., 2020; Cheng and Ferrell, 2019; 71 Fang and Newport, 1991; Murray and Kirschner, 1989).

72 The processes we chose to examine were protein synthesis and degradation, which are not only 73 potentially affected by the cytoplasmic protein concentration, but also directly involved in 74 determining the protein concentration. Xenopus extracts can carry out protein synthesis from 75 their own stores of mRNAs or from added synthetic mRNAs (Kanki and Newport, 1991; 76 Minshull et al., 1989; Ruderman et al., 1979), and they degrade both endogenous proteins (most 77 notably the various substrates of the APC/C) (Kamenz et al., 2021; King et al., 1996) and added 78 probe proteins [the present work]. In some ways, both *Xenopus* extracts and the eggs from which 79 they are derived represent unusual systems for studies of protein control. Transcription is largely

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80 absent from fertilized eggs and developing embryos until the midblastula transition (Amodeo et 81 al., 2015; Newport and Kirschner, 1982a, b), and the mRNA content is unchanging throughout 82 the cleavage stages of embryogenesis. In addition, although translational control is critical during 83 oocyte maturation and immediately after fertilization (Fox et al., 1989; Meneau et al., 2020; Paris 84 et al., 1988; Richter et al., 2007; Rosenthal et al., 1983), it appears not to be important during much of embryogenesis (Peshkin et al., 2015). In other ways, the dynamics of proteins in 85 86 Xenopus extracts are typical of animal cells. Common mammalian cell lines have protein 87 concentrations of about 75 mg/mL (Liu et al., 2022), as do Xenopus extracts (Murray, 1991), and 88 the median protein half-lives in Xenopus extracts (Peshkin et al., 2015) and mouse NIH3T3 cells 89 (Schwanhausser et al., 2011) are almost identical. The simplicity, manipulability, and 90 verisimilitude of the extract system makes it an attractive choice for the present studies of how protein synthesis and degradation are affected by the cytoplasmic concentration. 91 92 In this study, we directly manipulated the cytoplasmic macromolecule concentration and 93 viscosity of Xenopus egg extracts and assessed the immediate effects on protein synthesis and 94 degradation. We found that translation rates were maximal in 1x cytoplasmic extracts; translation 95 initially increased with cytoplasmic concentration, but then sharply decreased above 1x. Thus, 96 translation is an example of a process whose speed is in fact maximized at the normal 97 concentration of cytoplasmic macromolecules. In contrast, degradation rises with cytoplasmic 98 concentration until the concentration reaches almost 2x. The different concentration optima can 99 be explained by the sensitivities of the processes to viscosity; the viscogen Ficoll 70 was found 100 to be a more potent inhibitor of protein synthesis than of protein degradation. The differential 101 sensitivity of protein synthesis and protein degradation to viscosity provides a simple mechanism 102 for ensuring long-term protein concentration homeostasis.

103

#### 104 **Results**

#### 105 *Xenopus* egg extracts are robust towards cytoplasmic dilution and concentration.

106 The most commonly used types of extract are CSF (cytostatic factor)-arrested extracts,

- 107 interphase-arrested extracts, and cycling extracts (Cheng and Ferrell, 2019; Dunphy et al., 1988;
- 108 Murray, 1991; Newport and Spann, 1987). In pilot experiments we found that cycling extracts

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were the most reliable and longest lived, and so they were chosen for most of the experiments
that follow. One caveat is that previous work has shown that translation rates vary between
interphase and M-phase (Kanki and Newport, 1991), raising the concern that the time course of
protein synthesis would be characterized by alternations between different rates. This proved not
to be the case, possibly because mitosis sweeps through the extract in spatial waves (Chang and
Ferrell, 2013) (see Movies S1 and S2), so that both mitotic and interphase rates would probably
contribute to the measured rate of synthesis at all time points.

116 To alter the macromolecular concentration of cycling extracts, we used a spin-column with a 10

117 kilodalton (kDa) cutoff to produce a cytosolic filtrate and a cytoplasmic concentrate (Figure 1B).

118 The filtrate was found to be essentially protein-free by Bradford assay as well as by gel

electrophoresis and Trihalo compound or Coomassie staining (Figure 1C and S1). The retentate

120 was on average 2-fold concentrated compared to the starting cytoplasm by Bradford assay

121 (Figure 1C). We then diluted either the starting 1x extract or the 2x retentate with the filtrate to

122 generate extracts with a range of cytoplasmic macromolecule concentrations (Figure 1D, E).

123 We first examined the effects of concentration on two basic aspects of the extract's function: its 124 ability to self-organize and to cycle. The extract's gross organization was found to be remarkably 125 robust to cytoplasmic dilution (Figure 1D, E). Using a microtubule stain, SiR-tubulin, cell-like 126 compartments (Afanzar et al., 2020; Cheng and Ferrell, 2019) were found to form even when the 127 extract was diluted to as low as 0.3x (Figure 1D, E, and Movies S1-S3), in general agreement 128 with a previous report (Cheng and Ferrell, 2019), and to partially organize, with small asters, 129 even at 0.2x the normal cytoplasmic concentration (Movie S3). By following microtubule 130 polymerization and depolymerization, cell cycles were detected down to dilutions of 0.2x, and 131 the oscillations persisted for at least 14 hours with more than 10 complete periods (Figure 1C, D, 132 Movies S1-S3). In agreement with a previous study (Jin et al., 2022), the diluted extracts did not 133 show signs of significant cell cycle defects except that the duration of interphase and the cell 134 cycle period increased with increasing dilution.

135 On the other hand, the 2x retentate was stickier and more viscous than a 1x extract. Cell-like

136 compartments failed to form at concentrations higher than 1.4x (Figure 1E), and the cell cycle

137 appeared to be arrested above 1.4x. Nevertheless, when a 2x extract was diluted to 1.4x or less,

138 cell-like compartment formation was restored, and the cell cycle behavior was almost normal

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139 (Figure 1E), although dilutions from the 2x retentate had slightly longer interphases and were

140 slightly more susceptible to apoptosis than dilutions from a 1x extract (Figures 1D and E).

141 Overall, extracts were more sensitive to being concentrated than diluted, but even so, extracts

142 were able to carry out grossly normal self-organization and cycling over a wide range of

143 cytoplasmic concentrations.

#### 144 **Protein synthesis peaks at a 1x cytoplasmic concentration.**

145 To measure the protein synthesis rate, we added an mRNA for eGFP and monitored fluorescence 146 as a function of time. In pilot experiments, we titrated the mRNA concentration and found that 147 we could obtain a satisfactory signal without saturating the translation machinery using a 148 concentration of 2.5 ng/ $\mu$ L (Figure 2A). We then recorded time courses of eGFP fluorescence 149 intensity for diluted and concentrated extracts all with the same 2.5 ng/µL concentration of 150 mRNA for eGFP, and calculated translation rates from the linear portion of the time course 151 (Figure 2B). Figure 2C summarizes the data as directly obtained, with equal concentrations of 152 mRNA at each dilution but differing concentrations of the translation machinery. In principle, 153 calculated rates can be plotted against either relative cytoplasmic concentration using the average 154 fold relation from multiple experiments (Figure 1C) or absolute protein concentration measured 155 for each experiment. However, we observed that absolute protein concentration for individual 156 experiments was no better at addressing the variability among experiments than relative 157 cytoplasmic concentration (Figure S2). Furthermore, relative cytoplasmic concentration provides 158 a more straightforward theoretical treatment, as discussed later. Therefore, we opted to use 159 relative cytoplasmic concentration in instances where both relative cytoplasmic concentration 160 and protein concentration were viable options. Translation increased with cytoplasmic 161 concentration to a maximum at  $\sim 0.75x$  and fell thereafter. To relate this to endogenous 162 translation, given that the endogenous mRNAs would vary with concentration just as the 163 translation machinery does, we calculated an inferred endogenous translation rate, taken as the 164 observed translation rate multiplied by the cytoplasmic concentration. This is shown in Figure 165 2D; maximal translation was obtained at a cytoplasmic concentration of ~1x. We also calculated 166 the translation rate normalized for both equal ribosome concentration and equal mRNA 167 concentration, by dividing the raw translation rates by the cytoplasmic concentration (Figure 2E). 168 This provides an estimate of how the specific activity of the translation machinery is affected by

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169 cytoplasmic concentration. The inferred specific activity fell markedly with increasing

- 170 cytoplasmic concentration above 0.5x; below that there was too much variability to draw
- 171 conclusions. These findings show that protein synthesis is fastest in 1x cytoplasm, as predicted
- 172 by the maximal speed conjecture (Dill et al., 2011), and suggest that protein synthesis is inhibited
- 173 when the cytoplasmic viscosity is higher than normal. This latter point is explored further below.
- 174 As a second way of gauging the translation rate, we added equal concentrations of  $^{35}$ S-
- 175 methionine to extracts with a range of cytoplasmic concentrations and no added exogenous
- 176 mRNA, and measured <sup>35</sup>S incorporation into TCA-precipitable material. Figure 2F shows that
- 177 incorporation increased linearly with time through 75 min, and that the protein synthesis
- 178 inhibitor cycloheximide blocked this incorporation. Translation peaked at a cytoplasmic
- 179 concentration of ~0.8x (Figure 2G). Overall the dependence of translation on cytoplasmic
- 180 concentration was very similar to that seen with eGFP (Figure 2D and 2G), and again the
- 181 inferred specific activity of the translation machinery fell with cytoplasmic concentrations above
- 182 ~0.5x (Figure 2H). Thus the effects of cytoplasmic concentration seen with eGFP translation
- 183 appear to be applicable to translation from endogenous mRNAs as well.

#### 184 **Protein degradation peaks at a higher cytoplasmic concentration.**

185 As a first measure of protein degradation, we made use of an exogenous protein substrate, a 186 heavily BODIPY (boron-dipyrromethene)-labeled BSA, DQ-BSA (for dye-quenched bovine 187 serum albumin). This protein becomes fluorescent during degradation because the BODIPY 188 groups become dequenched. We carried out titration experiments, which showed that an 189 approximately linear response could be obtained with a DQ-BSA concentration of 5 µg/mL 190 (Figure 3A, B). This concentration was then used for experiments with extracts diluted to various 191 extents. As shown in Figure 3C, the rate of DQ-BSA dequenching increased with the 192 concentration of macromolecules and peaked at about 1.6x. The proteosome inhibitor MG132 193 blocked this dequenching, indicating that dequenching was largely due to proteosomes rather 194 than lysosomes. As we did for eGFP synthesis, we also multiplied the rate data by the extract 195 concentration to infer a degradation rate for endogenous proteins, where both the substrate and 196 the proteolysis machinery would be affected by cytoplasmic concentration; this shifted the 197 activity peak to  $\sim 1.8x$  (Figure 3D). Note that by paired *t*-test, the average for the 1.8x data was 198 not significantly higher than the average for the 2x data (p = 0.26 for a one-tailed *t*-test), so the

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optimal cytoplasmic concentration for DQ-BSA dequenching may actually be higher than 1.8x.
The specific activity calculation (Figure 3E) showed that the enzyme activity fell above ~1.4x
cytoplasmic concentration. At lower cytoplasmic concentrations, the relationship between this
gauge of activity and concentration was complicated; perhaps simple bimolecular kinetics do not
pertain in this regime.

204 As a second measure of protein degradation, we used a securin-CFP fusion protein as a reporter. 205 Securin is a cell cycle protein known to be targeted for proteasome-mediated protein degradation 206 by the anaphase promoting complex/cyclosome (APC/C) in late mitosis. We measured the decay 207 of securin-CFP fluorescent intensity and calculated the degradation rate (Kamenz et al., 2021) 208 for each of the dilution conditions (Figure 3F). As was the case with DQ-BSA dequenching, the 209 protein degradation rate peaked at a ~1.6x cytoplasmic macromolecular concentration (Figure 210 3G), and the inferred rate for a substrate being diluted along with the degradation machinery 211 peaked at 1.8x (Figure 3H). Again, by paired *t*-test, the average for the 1.8x data was not 212 significantly higher than the average for the 2x data (p = 0.34 for a one-tailed *t*-test), so the 213 optimal cytoplasmic concentration for securin-CFP degradation may be higher than 1.8x. The 214 inferred specific activity for securin-CFP degradation fell steadily with concentration (Figure 3I). 215 Thus, by both measures, protein degradation rates were maximal at a cytoplasmic concentration 216 of about 1.8x, higher than the optimal concentration for protein synthesis.

#### 217 Viscosity affects protein translation rate and, to a lesser extent, protein degradation.

218 The decrease in translation at high cytoplasmic macromolecule concentrations suggests that

translation is diffusion-controlled in a viscous cytoplasm, and that concentrated cytoplasm has a

220 higher viscosity that reduces the molecular movement necessary for the translation reaction. To

test these ideas, we first measured how diffusion coefficients vary with cytoplasmic

concentration. We used single particle tracking of fluorescently labeled PEGylated 100 nm

223 diameter polystyrene beads, which are comparable in size to some of the large complexes

involved in translation (Figure 4A). In 1x extracts, the motion of the beads was subdiffusive,

- with the diffusivity exponent  $\alpha$  to be 0.88 ± 0.06 (means ± S.E.) (Figure 4B, C). We calculated
- an average effective diffusion coefficient *D* from a fit of the random walk diffusion equation to
- the data over a time scale of 1 s. This was found to be  $0.36 \pm 0.23 \,\mu\text{m}^2/\text{s}$  (means  $\pm$  S.E.), in good

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agreement with previous studies (Delarue et al., 2018; Huang et al., 2022). There was substantial

- variability from position to position in the speed of diffusion (Figure 4B, insets, and 4C).
- 230 Similarly high variability has been reported for the diffusion of genetically-encoded
- 231 nanoparticles expressed in *S. pombe* (Garner et al., 2023), which is thought to reflect the
- 232 heterogeneity of the cytoplasmic environment.

233 The effective diffusion coefficient for the 100 nm beads varied dramatically with cytoplasmic

- concentration; it was ~11x higher in filtrate (0x cytoplasm) compared to 1x extracts, and ~11x
- lower in 2x extracts. The measured diffusion coefficients obeyed Phillies's law (Phillies, 1986;
- 236 Phillies, 1988):

237 
$$D[\phi] = D[0]e^{-\mu\phi},$$
 [Eq. 1]

238 where  $D[\phi]$  is the diffusion coefficient at a relative cytoplasmic concentration  $\phi$ , D[0] is the

239 diffusion coefficient in filtrate, and  $\mu$  is a scaling factor that depends upon the size of the probe.

240 A similar relationship between diffusion coefficients and macromolecular concentration has been

observed for large multimeric protein complexes (Alric et al., 2022; Molines et al., 2022).

242 Similarly, the scaling factor varied approximately linearly with the measured size of the beads

243 (Figure 4D) (Alric et al., 2022). Thus, diffusion was markedly affected by changing the

244 cytoplasmic macromolecule concentration over a 0x to 2x range, and the changes were greatest245 for large probe particles.

Next, we diluted extracts to 0.7x, 0.8x, or 0.9x, and altered the cytoplasmic viscosity by adding

Ficoll 70, a protein-sized (70 kDa) carbohydrate that can act both as a crowding agent and a

248 viscogen (Figure 4G). The effective diffusion coefficients were found to decrease with

249 increasing Ficoll concentration; 6% Ficoll 70 decreased the diffusion coefficient for a 40 nm

bead by a factor of 33, and 2-3% Ficoll 70 yielded diffusion coefficients comparable to those

251 measured in 2x cytoplasm. Thus, Ficoll can be used to bring about the marked changes in

viscosity seen when cytoplasm is concentrated, without changing protein concentration.

We therefore asked whether this range of Ficoll 70 concentrations would inhibit proteinsynthesis and degradation. Note that Ficoll might be expected to have either of two opposite

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255 effects on enzyme reaction rates: by acting as a crowding agent, it increases the concentrations of 256 the reactants and thus could increase the rate of a reaction; but by acting as a viscogen, it could 257 slow protein motions and decrease in the reaction rate. In vitro studies have shown that either of 258 these effects can predominate (Aoki et al., 2013; Minton, 2001; Tan et al., 2013). We found that 259 the rate of translation of eGFP monotonically decreased with increasing Ficoll 70 concentration, 260 with an IC50 of ~2-3% (Figure 4H). Diffusion coefficients in these Ficoll-supplemented 0.7x to 261 0.9x extracts supplemented with 2-3% Ficoll 70 were similar to those seen in 2x extracts with no 262 Ficoll. Thus protein synthesis is sensitive to viscosity over a range relevant to the cytoplasmic 263 concentration/dilution experiments.

The rate of DQ-BSA unquenching was substantially less sensitive to viscosity (Figure 4I), with an IC50 greater than 6% Ficoll 70. Thus, both protein synthesis and protein degradation, as measured by the eGFP and DQ-BSA assays, are sensitive to the viscosity of the cytoplasm, with synthesis being more sensitive than degradation. This difference in sensitivity is sufficient to account for the different optimal cytoplasmic concentrations found for translation and degradation.

#### 270 A model for the effect of diffusion on reaction rates

Final, we asked whether we could derive a simple model to account for the observed rates of protein translation and degradation as a function of cytosolic protein concentration. In particular, we wished to see if plausible assumptions could account for the biphasic nature of the curves, and to explore how differences in the kinetics of translation vs. degradation might account for the differences in their concentration optima.

We assume that the rate determining reaction for each process is a mass action bimolecularreaction:

278 
$$V = \frac{dP}{dt} = kE \cdot S$$
 [Eq 2]

where V is the rate of the reaction, P is the product of the reaction, E is the enzyme, S the substrate, and P the product of the reaction. Alternatively, we could assume a two-step, saturable mechanism (see Supplementary Information), but the mass action treatment suffices for present

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purposes and is simpler. The enzyme and substrate concentrations are linearly proportional to the relative cytoplasmic concentration  $\phi$ . We can therefore write:

$$E[\phi] = \phi E[1]$$
 [Eq. 3]

285 
$$S[\phi] = \phi S[1],$$
 [Eq. 4]

where  $E[\phi]$  and  $S[\phi]$  are the enzyme and substrate concentrations at a relative cytoplasmic concentration of  $\phi$ , and E[1] and S[1] are the enzyme and substrate concentrations at a relative cytoplasmic concentration 1x. Substituting into Eq. 2 yields:

289 
$$V = k\phi^2 E[1]S[1].$$
 [Eq. 5]

290 Next we consider the dependence of the rate constant on the cytoplasmic protein concentration.

291 From the Smoluchowski equation (Smoluchowski, 1917), the collision rate and the association

rate constant k are proportional to the sum of the diffusion coefficients of E and S, and from

Phillies's law (Eq. 1) (Phillies, 1986; Phillies, 1988), we take the diffusion coefficients to be
negative exponential functions of the cytoplasmic protein concentration:

295 
$$k[\phi] \propto D_E[\phi] + D_S[\phi] = D_E[0]e^{-\mu_E\phi} + D_S[0]e^{-\mu_S\phi},$$
 [Eq. 6]

where  $D_E[0]$  and  $D_S[0]$  are the diffusion coefficients of the enzyme and the substrate at a cytoplasmic concentration of 0 (i.e. in filtrate), and the  $\mu$ 's are scaling factors. For the special case where either one diffusion coefficient is much smaller than the other, or the scale factors are equal, we can simplify this to:

300  $k[\phi] = k[0]e^{-\mu\phi}$ . [Eq. 7]

301 Note that it is a bit awkward to consider a value of k at a relative cytoplasmic concentration of 0, 302 since the reacting species are cytoplasmic macromolecules that are absent from the filtrate. We 303 can avoid this by instead writing:

304

$$k[\phi] = k[1]e^{-\mu(\phi-1)}.$$
 [Eq. 8]

305 It follows that:

306 
$$V = k[1]E[1]S[1](\phi^2 e^{-\mu(\phi-1)}).$$
 [Eq. 9]

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Finally, we can make use of the fact that the scaling factor  $\mu$  is linearly proportional to the size of the diffusing particle  $d_p$ , and write an expression that explicitly acknowledges particle size:

309 
$$V = k[1]E[1]S[1](\phi^2 e^{-ad_p(\phi-1)}).$$
 [Eq. 10]

where *a* is a new scaling factor that relates  $d_p$  to  $\mu$ . Eq. 10 describes how the rate of a mass action, bimolecular reaction whose reactants obey Phillies's law and mass would be expected to vary with the cytoplasmic macromolecule concentration and molecular diameter. If we measure rates in arbitrary units with the rate at  $\phi = 1$  taken as 1, then:

314 
$$V = \phi^2 e^{-ad_p(\phi-1)}$$
. [Eq. 11]

Note that we have an experimental estimate for *a* (which, from Figure 4F is 0.018 nm<sup>-1</sup>), leaving only one adjustable parameter,  $d_p$ , the macromolecular diameter. Eq. 11 defines a biphasic, nonmonotonic curve (Figure 5A), and the larger the assumed macromolecular diameter, the further to the left the curve's maximum lies (Figure 5A). For a given value of  $d_p$ , the optimal

319 cytoplasmic concentration is given by:

320 
$$\phi_{optimal} = \frac{2}{ad_p}.$$
 [Eq. 12]

The experimentally observed rates for translation and degradation are well captured by Eq. 11, with the fitted values of  $d_p$  being  $104 \pm 2$  nm for translation and  $14 \pm 1$  nm for degradation (means  $\pm$  S.E.) (Figure 5C).

The result is a dynamical system that will be in steady state—the translation and degradation rates will be equal—at a relative cytoplasmic concentration of 1x. Moreover, the steady state is guaranteed to be stable. If the system is perturbed such that the cytoplasmic concentration exceeds 1x, then the degradation rate will rise and the translation rate will fall, driving the system back toward the 1x steady state (Figure 5C). Conversely, if the cytoplasmic concentration falls below 1x, the translation rate will exceed the synthesis rate, again driving the system back toward the physiological set point (Figure 5C).

#### 331 Discussion

Here we have tested the hypothesis that the concentration of macromolecules in the cytoplasm isset to maximize the rates of important biochemical reactions. We found that in cycling *Xenopus* 

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334 egg extracts, the rate of translation, as measured by the synthesis of eGFP from an exogenous mRNA and the incorporation of <sup>35</sup>S-methionine into endogenous translation products, does peak 335 336 at a 1x cytoplasmic concentration, consistent with the maximal speed hypothesis (Figure 2). This 337 finding fits well with previous studies of cost minimization and near-optimal resource allocations 338 in models of *E. coli* protein synthesis (Hu et al., 2020; Klumpp et al., 2013; Scott et al., 2014). 339 However, protein degradation, as measured by DQ-BSA dequenching and CFP-securin 340 degradation peaks at a higher cytoplasmic concentration, ~1.8x (Figure 3). The difference in 341 concentration optima can be explained by the differences in the sensitivities of translation vs. 342 degradation to viscosity: the viscogen Ficoll 70 is more potent in inhibiting translation than 343 degradation (Figure 4H, I). This in turn may be due to differences in the sizes of the 344 macromolecular complexes involved in the two processes, as the diffusion coefficients for large 345 fluorescent beads are more affected by cytoplasmic concentration than those of smaller beads 346 (Figure 4E, F). Other factors that might make translation be more diffusion-limited than protein degradation could also contribute the differential sensitivity of the two processes to changes in 347 348 cytoplasmic concentration. The different optimal cytoplasmic concentrations for translation vs. 349 degradation mean that the system is homeostatic: increasing the concentration of 350 macromolecules in the cytoplasm would increase the rate of degradation and decreases the rate 351 of translation, whereas decreasing the cytoplasmic concentration would decrease the rate of 352 degradation (Figure 5). This behavior can be explained through a theoretical treatment based on mass action kinetics and Phillies's law (Phillies, 1986; Phillies, 1988). 353 354 Both the mRNA translation and protein degradation rates measured here were found to smoothly 355 vary with cytoplasmic concentration (Figures 2 and 3). Thus, there was no evidence for critical

356 concentrations above or below which the processes abruptly ceased. We suspect that any such

357 critical points lie outside the range of concentrations examined here. Likewise, the effects of high

358 cytoplasmic concentration on translation and degradation dynamics appeared to be largely

reversible, since the activities measured in a 2x extract diluted back to 1x were very similar to

360 those in the original 1x extract (Figures 2 and 3).

361 Although the conventional wisdom is that almost all biochemical reactions are reaction-

- 362 controlled (i.e., the catalytic rate constant  $k_2$  is much smaller than  $k_{-1}$ ) rather than diffusion
- 363 controlled ( $k_{-1}$  is much smaller than  $k_2$ ) (Bar-Even et al., 2011; Davidi et al., 2016), both of the

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364 processes measured here were inhibited by the crowding agent/viscogen Ficoll 70, with 365 translation substantially more sensitive than degradation. The simplest interpretation is that 366 translation (in particular) is running relatively close to the diffusion limit, possibly because in the 367 extract, the diffusion of large macromolecules required for dissociation  $(k_{-1})$  is quite slow. 368 Note that the shapes of the rate curves mean that protein synthesis and degradation can be 369 viewed as a negative feedback system. Increasing the cytoplasmic protein concentration 370 increases the cytoplasmic viscosity, which negatively affects translation, which makes the 371 protein concentration eventually drop-a negative feedback loop based on the sensitivity of 372 translation to viscosity. Conversely, decreasing the cytoplasmic protein concentration decreases 373 the cytoplasmic viscosity, which mitigates the drop in translation rates that would normal be 374 expected from a decrease in ribosome and mRNA concentration. Such feedback regulation may 375 also pertain to the oscillation of biomass growth rate and maintenance of cytoplasmic density 376 found in single mammalian cells (Liu et al., 2020). Negative feedback is a common theme in 377 homeostatic systems. This process can alternatively be viewed as a variation on end product 378 inhibition, where the product of protein synthesis inhibits translation, but through the 379 intermediacy of changes in protein diffusion rates rather than through the direct binding of the 380 product to the enzyme.

381 We do not yet have direct evidence for the time scale of this proposed protein concentration 382 homeostasis. Based on the measurement of 43 h for the median half-life of a *Xenopus* protein 383 during embryogenesis (Peshkin et al., 2015), we suspect that the response might require tens of 384 hours. This time scale would be particularly appropriate for protein homeostasis in the immature 385 oocyte, the egg's immediate precursor in development. The oocyte is thought to live for weeks or 386 months in the frog ovary and to vary little in terms of size, appearance, and composition during 387 this time (Ferrell, 1999; Smith et al., 1991). In contrast, the changes in protein synthesis and 388 degradation are likely to be too slow make a significant impact during the decrease in 389 cytoplasmic concentration that occurs during mitosis, since embryonic mitosis is only about 15 390 min in duration.

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#### **393** Author contributions

- 394 Conceptualization, Y.C., J.H., and J.E.F.; Methodology, Y.C., J.H, C.P., and J.E.F.; Software,
- 395 Y.C.; Formal Analysis, Y.C. and J.E.F.; Investigation, Y.C.; Resources, C.P.; Writing Original
- 396 Draft, Y.C. and J.E.F.; Visualization, Y.C. and J.E.F.; Supervision, J.E.F.; Funding Acquisition,
- 397 J.E.F.

#### **398 Declaration of interests**

399 The authors declare no competing interests.

400



# Figure 1. General properties of diluted and concentrated *Xenopus* egg extracts: effects on self-organization and cycling

405 (A) Schematic view of protein synthesis and degradation.

406 (B) Preparation of *Xenopus* egg extract, 2x concentrated retentate, and protein-depleted filtrate.

407 (C) Protein concentration in extract, retentate, and filtrate. Concentrations were determined by

Bradford assays. Data are from five extracts. Individual data points are overlaid with the meansand standard errors.

410 (D) SiR-tubulin staining (left) and SiR-tubulin fluorescence intensity as a function of time (right)
411 in an extract after various dilutions. The starting material was a 1x extract, diluted with various

412 proportions of filtrate and imaged in a 96-well plate under mineral oil. All fields are shown at

413 equal exposure. The fluorescence intensities shown on the right were quantified from the center

414 1/9 of the wells.

415 (E) SiR-tubulin staining (left) and SiR-tubulin fluorescence intensity as a function of time (right)

416 in an extract after various dilutions. The data were collected as in (D) except that the starting

417 material was a 2x extract.

17





420 Figure 2. The rate of mRNA translation is maximal at a cytoplasmic concentration of ~1x.

421 (A) Titration of mRNA concentration for eGFP expression. The indicated concentration (2.5

422  $\mu g/mL$ ) was chosen for the experiments in (B-E).

423 (B) eGFP expression as a function of time for various dilutions of a 1x extract.

424 (C) Translation rate as a function of cytoplasmic concentration. These are the directly-measured

425 data from experiments where the eGFP mRNA concentration was kept constant and the

426 translation machinery was proportional to the cytoplasmic concentration. Data are from 6

- 427 experiments for dilution from 1x extracts and 7 experiments for dilution from 2x retentates. Data
- 428 are normalized relative to the translation rates at a cytoplasmic concentration of 1x. Means and
- 429 standard errors are overlaid on the individual data points. In this and the subsequent panels, the
- 430 darker green represents data from diluting 2x retentates and the lighter green from diluting 1x
- 431 extract.

- 432 (D) Inferred translation rates for the situation where the mRNA concentration as well as the
- 433 ribosome concentration is proportional to the cytoplasmic concentration. The rates from (C) were
- 434 multiplied by the relative cytoplasmic concentrations.
- 435 (E) Inferred translation rates for the situation where both the mRNA concentration and the
- 436 ribosome concentration are kept constant at all dilutions. The rates from (C) were divided by the
- 437 relative cytoplasmic concentrations.
- 438 (F) TCA-precipitable <sup>35</sup>S incorporation as a function of time for translation from endogenous
- mRNAs. Various dilutions of a 1x extract are shown. CHX denotes a 1x extract treated with 100
  µg/mL cycloheximide.
- 441 (G) Inferred translation rates for the situation where mRNA concentration is kept constant and
- 442 ribosome concentration is proportional to the cytoplasmic concentration. The rates from (H)
- 443 were divided by the relative cytoplasmic concentration. The grey data points are from CHX (100
- 444  $\mu g/mL$ )-treated 1x extracts.
- 445 (H) Translation rate as a function of cytoplasmic concentration. These are the directly-measured
- 446 data from experiments where the <sup>35</sup>S concentration was kept constant but both the (endogenous)
- 447 mRNA concentration and translational machinery were proportional to the cytoplasmic
- 448 concentration. Data are from 3 experiments for dilution from 1x extracts and 3 experiments for
- dilution from 2x retentates. Data are normalized relative to the translation rates at a cytoplasmic
- 450 concentration of 1x. Means and standard errors are overlaid on the individual data points.
- 451 (I) Inferred translation rates for the situation where both the mRNA concentration and the
- 452 ribosome concentration are kept constant at all dilutions. The rates from (H) were divided twice
- 453 by the relative cytoplasmic concentrations (i.e. by the relative concentration squared).

19



455 Figure 3. The rate of protein degradation is maximal at cytoplasmic concentrations of
456 ~1.8x.

457 (A) Titration of substrate protein concentration for DQ-BSA degradation experiments. The

458 indicated concentration (5  $\mu$ g/mL) was chosen for the experiments in (B-E).

(B) DQ-BSA fluorescence as a function of time for various dilutions of a 1x extract.

460 (C) Degradation rate as a function of cytoplasmic concentration. These are the directly-measured

461 data from experiments where the DQ-BSA concentration was kept constant and the proteolysis

- 462 machinery was proportional to the cytoplasmic concentration. The grey data points denoted
- 463 MG132 are from 1x extracts treated with 200  $\mu$ M MG132, a proteosome inhibitor. Data are from
- 464 4 experiments for dilution from 1x extracts and 4 experiments for dilution from 2x retentates.
- 465 Data are normalized relative to the degradation rates at a cytoplasmic concentration of 1x. Means
- and standard errors are overlaid on the individual data points. In this and the subsequent panels,
- the darker purple represents data from diluting 2x retentates and the lighter purple from diluting
- 468 1x extract.

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#### 469

470 (D) Inferred degradation rates for the situation where the substrate concentration as well as the
471 proteosome concentration is proportional to the cytoplasmic concentration. The rates from (C)
472 were multiplied by the relative cytoplasmic concentrations.

473 (E) Inferred degradation rates for the situation where both the substrate concentration and the

474 proteosome concentration are kept constant at all dilutions. The rates from (C) were divided by

475 the relative cytoplasmic concentrations.

476 (F) Degradation of securin-CFP as a function of time for various dilutions of a 1x extractt.

477 (G) Degradation rate as a function of cytoplasmic concentration. These are the directly-measured

478 data from experiments where the securin-CFP concentration was kept constant but the

479 proteosome concentration was proportional to the cytoplasmic concentration. Data are from 4

480 experiments for dilution from 1x extracts and 4 experiments for dilution from 2x retentates. Data

481 are normalized relative to the degradation rates at a cytoplasmic concentration of 1x. Means and

482 standard errors are overlaid on the individual data points.

483 (H) Inferred degradation rate for the situation where both the substrate and proteosome

484 concentrations are proportional to the cytoplasmic concentration. The rates from (G) were

485 multiplied by the relative cytoplasmic concentrations.

486 (I) Inferred degradation rates for the situation where both the substrate and the proteosome

487 concentration are kept constant at all dilutions. The rates from (G) were divided by the relative

488 cytoplasmic concentrations.







492 (A) The sizes of various macromolecules and complexes involved in translation and degradation.

- 493 (B) Single particle traces for diffusion of 100 nm fluorescent beads in 1x cytoplasmic extracts.
- 494 Two examples of location-to-location variability are highlighted.
- 495 (C) Mean-squared displacement for 110 individual trajectories (black) and average mean-squared
- 496 displacement (red) as a function of the time difference τ. Effective diffusion coefficients were
- 497 calculated from the first 1 s of data.

Α

22

498 (D) Effective diffusion coefficients for 100 nm fluorescent beads as function of relative

499 cytoplasmic concentration. Data are from 3 experiments for the 2x extract dilution and from 2

500 experiments for the 1x extract dilution. Error bars for the 2x extract dilution represent means  $\pm$ 501 standards errors.

502 (E) Effective diffusion coefficients for beads of different diameter (nominally 40 nm, 100 nm,

and 200 nm) as a function of relative cytoplasmic concentration. Data are from 3 experiments.

504 Means and standard errors are overlaid on the individual data points.

505 (F) The scaling factor  $\mu$  (from Eq. 1) as a function of bead diameter. The apparent bead

506 diameters (nominally 40, 100, and 200 nm) were calculated from their diffusion coefficients in

507 extract buffer with no sucrose using the Stokes-Einstein relationship. Scaling factors are from 3

508 experiments and are shown as means  $\pm$  S.E. Bead diameters are from 3 experiments for the 40

509 nm beads and 4 experiments for the 100 and 200 nm beads, and again are plotted as means  $\pm$  S.E.

510 The diameters of proteosomes and polyribosomes are shown for comparison.

511 (G) Diffusion coefficients of 40 nm beads as a function of Ficoll 70 concentration. Extracts were

512 prepared at 0.7x, 0.8x, and 0.9x as indicated and supplemented with Ficoll to yield the final

513 concentrations (w/vol) shown on the x-axis. Data are from 3 experiments. Means and standard

514 errors are overlaid on the individual data points. Diffusion coefficients for the undiluted 1x

515 extracts were also measured and the average is shown for reference.

516 (H) Translation rates, using the eGFP assay, as a function of Ficoll 70 concentration. Extracts

517 were prepared at 0.7x, 0.8x, and 0.9x as indicated and supplemented with Ficoll to yield the final

518 concentrations (w/vol) shown on the x-axis. Data are from the same 3 experiments shown in (G).

519 Means and standard errors are overlaid on the individual data points. Translation rates for the

520 undiluted 1x extracts were also measured and the average is shown for reference.

(I) Degradation rates, using the DQ-BSA assay, as a function of Ficoll 70 concentration. Extracts
were prepared at 0.7x, 0.8x, and 0.9x as indicated and supplemented with Ficoll to yield the final
concentrations (w/vol) shown on the *x*-axis. Data are from the same 3 experiments shown in (G).
Means and standard errors are overlaid on the individual data points. Degradation rates for the
undiluted 1x extracts were also measured and the average is shown for reference.





Figure 5. Homeostasis in a model of the effect of cytoplasmic concentration of translation
and protein degradation.

- 530 (A) Plot of Eq. 11, which relates a bimolecular reaction rate to the relative cytoplasmic
- 531 concentration, for various sizes of proteins. We assumed a = 0.018 nm<sup>-1</sup> (from Figure 4F).
- 532 (B) Calculated optimal relative cytoplasmic concentration for proteins of different assumed sizes, 533 again accuming  $a = 0.018 \text{ nm}^{-1}$
- 533 again assuming  $a = 0.018 \text{ nm}^{-1}$
- 534 (C) Fits of Eq. 11 to the experimental data for translation (green) and degradation (purple) as a
- 535 function of cytoplasmic concentration, calculated assuming that both the substrate and enzyme
- varied with the cytoplasmic concentration. All of the data from Figures 2D, H and 3D, H were
- 537 included in the fits. The  $R^2$  values are 0.92 for the translation data and 0.95 for the degradation
- 538 data. The fitted values for the size of the proteins involved are  $104 \pm 2$  nm (mean  $\pm$  S.E.) for
- translation and  $14 \pm 1$  nm (mean  $\pm$  S.E) for degradation. The fitted optimal cytoplasmic
- 540 concentrations are  $1.07 \pm 0.02$  for translation and  $8.1 \pm 0.8$  for degradation (mean  $\pm$  S.E.).
- 541

#### 24

#### 542 Star Methods

#### 543 Extract preparation

544 Cycling extracts were prepared as described previously (Chang and Ferrell, 2018; Murray, 1991) 545 with the following modifications. Briefly, freshly laid frog eggs were collected, washed with 20 546 g/L L-cysteine pH 7.8, and incubated for 3-5 min to remove the jelly coat. The eggs were then 547 washed twice with ~150 mL 0.2x 6s (MMR) solution (20 mM NaCl, 1 mM HEPES, 400 µM 548 KCl, 400 µM CaCl<sub>2</sub>, 200 µM MgCl<sub>2</sub>, and 20 µM EDTA pH 7.8) and resuspended in 50 mL 0.2x 549 MMR solution. Calcium ionophore A23187 (C7522, Sigma) was added to a final concentration 550 of 0.5  $\mu$ g/mL to activate the eggs. After 2 min of activation, liquid was removed, and the eggs 551 were washed twice with ~150 mL 0.2xMMR solution and three times with ~150 mL extract 552 buffer [100 mM KCl, 50 mM sucrose, 10 mM HEPES pH 7.7 (with KOH), 1 mM MgCl<sub>2</sub>, and 553 100 µM CaCl<sub>2</sub>]. Twenty min after activation (>80% of the eggs showed contraction of the 554 animal pole), the eggs were transferred to a 14 mL round-bottom polypropylene tube (352059, 555 Corning) and packed for 1 min at  $300 \times g$ . Excess liquid on top of the eggs was removed, and the 556 egg-containing tube was chilled on ice. The eggs were crushed by centrifugation at  $16,000 \times g$ 557 for 15 min at 4°C. The cytoplasmic layer was then collected by puncturing the side of the 558 extract-containing tube at  $\sim 2$  mm above the interphase between the extract layer and the yolk 559 layer. The extract was allowed to flow into a collecting Eppendorf tube by gravity or by gently 560 pressing the tube opening with one finger to create a positive pressure inside the tube. The 561 collected extract was mixed with 10  $\mu$ g/mL leupeptin, 10  $\mu$ g/mL pepstatin, 10  $\mu$ g/mL 562 chymostatin, and 10  $\mu$ g/mL cytochalasin B, and further refined by centrifugation at 16,000 × g 563 for 5 min at 4°C using a tabletop refrigerated centrifuge. After the refining centrifugation, the 564 clarified extract was transferred to a new tube.

565 CSF extracts (Kamenz et al., 2021; Murray, 1991) were prepared similarly to cycling extracts,

566 with the differences being that the eggs were washed with  $\sim$ 150 mL CSF extract buffer (100 mM

567 KCl, 50 mM sucrose, 10 mM potassium HEPES pH 7.7, 5 mM EGTA pH 7.7, 2 mM MgCl<sub>2</sub>, and

568 0.1 mM CaCl<sub>2</sub>) four times immediately after dejellied, without 0.2x MMR washes or calcium

569 ionophore activation. The whole process between dejelying and the crushing spin typically took

 $570 \sim 10$  min. After the refining centrifugation, the extract was transferred to a new tube and

571 supplemented with 100  $\mu$ g/mL cycloheximide.

#### 572 Filtrate and retentate preparation

- 573 Extract (400 µL) was transferred to a 10 kDa molecular weight cut-off centrifugal filter unit
- 574 (UFC501096, Millipore) placed in a collection tube and centrifuged at  $16,000 \times g$  for 10 min at
- 575 4°C three times. After each centrifugation period, the extract was taken out of the centrifuge and
- 576 mixed by pipetting. The filtrate was collected in the collection tube, and the retentate was
- 577 collected from the filtration unit.

#### 578 SiR-tubulin intensity

- 579 To monitor microtubules in cycling extracts, 200 nM SiR-tubulin was added to the extract,
- 580 retentate, and filtrate. Then the extract or retentate was mixed with different volume fractions of
- 581 filtrate to create a series of dilution conditions. Five µL of the dilutions were loaded onto a 96
- 582 well polystyrene assay plate (3368, Corning) and gently spread using the pointed end of the
- 583 loading pipette tip to allow even coverage of extract at the bottom of the well. A layer of 100 μL
- heavy mineral oil (330760, Sigma) was pipetted to cover the extract and prevent evaporation.
- 585 The 96 well plate was immediately loaded onto an inverted epi-fluorescence microscope (DMI8,
- 586 Leica) for imaging at a frame rate of  $0.5 \text{ min}^{-1}$ . The median intensity from the center 1/9 of each
- 587 frame was measured and plotted with off-sets in Figures 1D and 1E.

#### 588 eGFP translation and DQ-BSA degradation

- 589 For eGFP translation and DQ-BSA degradation experiments, the extract, filtrate, or retentate was
- 590 mixed with 2.5 ng/µL (unless otherwise stated) eGFP mRNA (L-7201-100, Trilink
- 591 Biotechnologies) or 5 ng/ $\mu$ L DQ-BSA (D12050, Thermo Fisher) on ice. The extract or retentate
- 592 was mixed with different proportions of the filtrate to generate different dilutions. The dilutions
- 593 (15 µL) were then added to a clear bottom 384-well plate (324021, Southern Labware) and
- 594 equilibrated to room temperature. The imaging plate was then loaded onto an inverted
- fluorescence microscope for time course measurements at a frame rate of 1 min<sup>-1</sup> or 0.5 min<sup>-1</sup>.
- 596 To calculate the rate of eGFP protein synthesis and DQ-BSA degradation, the median intensity
- 597 of the center quarter of each frame was measured. The raw rates were extracted by calculating
- 598 the slope of a linear segment from the intensity-time plot. The linear segment was typically
- 599 between 50 and 120 min for eGFP translation, and between 25 and 120 min for DQ-BSA
- 600 degradation experiments. Intensity trajectories were manually inspected and the linear segments

26

601 were adjusted individually to ensure linearity. The raw rates from dilutions of 1x extract (or 2x

retentate) were normalized by the rate measured in the original 1x extract (or the reconstituted 1x

603 extract) from the same batch of eggs to control for variability due to batch variation of the eggs

and experimental conditions, allowing comparison among experiments.

#### 605 <sup>35</sup>S-methionine labeling

606 A cycling extract was concentrated as described above. The extract, retentate, and filtrate were

supplemented with 1% v/v  $^{35}$ S-methionine to a final concentration of ~0.5  $\mu$ Ci/ $\mu$ L. The filtrate

608 was then mixed with different volume fractions of extract or retentate to generate a series of

609 dilutions. For the "CHX" sample, 100 µg/mL cycloheximide was added to a 1x extract. The

610 extract was then sampled at 15-min intervals, and the translation process was halted by directly

611 mixing 5  $\mu$ L samples with 100  $\mu$ L H<sub>2</sub>O, which was then mixed with 100  $\mu$ L 50% TCA

612 (trichloroacitic acid, T0699, Sigma). To collect and clean up the TCA precipitable material, 50

613 µL of the homogeneous extract/TCA mixture was passed through a glass fiber filter

614 (WHA1820025, Sigma) prewetted with 5% TCA, then 1 mL of 5% TCA was passed through the

615 filter to remove soluble material, and the filter was washed with 2 mL of 95% ethanol and dried

616 on vacuum. The filter with collected material was dropped into a 20-mL scintillation vial (03-

617 337-2, Thermo Fisher) containing 10 mL scintillation fluid (111195, RPI Research Products).

618 The radioactivity was measured using a liquid scintillation counter. The rate was calculated

619 similarly to the eGFP translation and DQ-BSA degradation experiments.

#### 620 Securin-CFP degradation

621 The securin-CFP degradation experiments followed a previous protocol (Kamenz et al., 2021)

622 with modifications. The fluorescent probe, securin-CFP, was made by mixing 10 µg of an SP6-

623 securin-CFP plasmid in 20 μL H<sub>2</sub>O with 30 μL SP6 High-Yield Wheat Germ Protein Expression

624 System (TnT® L3261, Promega), and incubating at room temperature for 2 h per the

625 manufacturer's instructions. CSF extracts were used for these experiments. The CSF extract was

626 additionally supplemented with purified recombinant nondegradable  $\Delta 90$  sea urchin cyclin B

627 protein at a concentration capable of driving the extract into an M-phase arrest and incubated at

628 room temperature for 30 min. 0.8 mM CaCl<sub>2</sub> was added to the extract and incubated for an

629 additional 30 min to degrade endogenous cyclin B. The extract was then divided into two

27

630 fractions, one kept on ice and the other concentrated using the previously stated method. A series 631 of dilutions were reconstituted by mixing the filtrate with either the extract kept on ice or 632 retentate from the concentrator. 19  $\mu$ L of the extracts were added and mixed with 1  $\mu$ L of the in 633 vitro transcribed and translated securin-CFP and pipette into a glass-bottomed 384-well plate. As 634 a background control, we also included a well of extract with no securin-CFP. The time courses 635 of fluorescence intensity were recorded using a fluorescence plate reader at a rate of 2 min<sup>-1</sup>. 636 To calculate the degradation rate, each experimental reading was subtracted by the 637 corresponding background measurement. The first few data points typically increased with time, 638 possibly due to equilibration of the fluorophore. Therefore, instead of normalizing to the first 639 data point in each time series, the background corrected intensities were divided by the

- 640 maximum of the first 15 time points (7.5 min). The normalized intensities were fitted to A = A[0]
- 641  $e^{-kt}+C$ , where A is the fluorescence, k is the rate constant, and t is time, and A[0] (constrained to
- be greater than 0.95), k, and C (constrained between 0 and 0.05) are fitting variables. The value
- 643 of k measured for each dilution condition from 1x extract (or from 2x retentate) was normalized
- to 1x extract (or nominal 1x reconstituted from the 2x retentate) from the same experiment to
- 645 control for variations among batches of eggs.

#### 646 Single particle tracking

- 647 PEGylated fluorescent particles were prepared by mixing 50  $\mu$ L of 20 mg/mL
- $648 \qquad methoxy polyethylene glycol amine 750 (07964, Sigma), 5 \ \mu L \ of fluorescent polystyrene nano$
- beads (2% solid, F8888 and F8795, Thermo Fisher), 50  $\mu L$  of 30 mM N-
- $\label{eq:main} 650 \qquad hydroxysulfosuccinimide~(56485, Sigma)~in~200~mM~borate~buffer~pH8.2, and~10~\mu L~of~100~mM$
- 651 N-(3-dimethylaminopropyl)-N'-ethylcarbodiimide hydrochloride (03450, Sigma). The
- 652 PEGylation reaction was incubated at room temperature for 20 h. The reaction was then stopped
- by 1:100 dilution with water, dialysis with 3 M NaCl, and three subsequent dialyses with water.
- The particles were diluted further to make it so that a 1:100 dilution provided a suitable
- 655 concentration for segmentation and tracking. 1:100 (v:v) of the beads were mixed into the extract
- by pipetting. 5  $\mu$ L of the extract was placed in the center of a well in a glass-bottom 96-well
- 657 plate. The plate was loaded onto an inverted epifluorescence microscope. The extract was
- allowed to equilibrate with the environment for 5 min, and a movie was taken at the appropriate
- 659 wavelength at a frame rate of 3 Hz using a 40x objective.

28

660 The time-lapse videos of particle movements were analyzed with a custom Python script.

- Briefly, the images were flat field corrected (background flat fields were generated using BaSiC,
- an ImageJ package) and bleach corrected. The particles were called and linked using the Trackpy
- 663 library with adaptive mode, which allows calling particle movements with large step size
- variations. Typical starting parameters for Trackpy were: diameter = 15, maxsize = 7, minmass =
- 665 650, search\_range =30, ecc\_threshold = 1, percentile = 99.5, topn = 300, memory = 1; drift
- 666 correction was typically off unless the movie had a translational flow. Movies were discarded if
- they contained a strong convergent or divergent flow. Parameters were adjusted for individual
- movies to allow capturing the greatest number of tracks without sacrificing tracking quality. The
- 669 mean squared displacement for an individual trajectory was calculated by  $(n\Delta t) =$

670 
$$\frac{1}{N-n-1} \sum_{i=1}^{N-n-1} [x(i\Delta t + n\Delta t) - x(i\Delta t)]^2 + [y(i\Delta t + n\Delta t) - y(i\Delta t)]^2$$
, where N is the number

- 671 of frames in a trajectory and x and y are the coordinates at  $i\Delta t$  or  $i\Delta t + n\Delta t$ . The ensemble mean 672 squared displacement was calculated by  $(n\Delta t) = \sum_{i=1}^{K} (N_i - n - 1) MSD_i(n\Delta t)$ , where K is the
- 673 number of trajectories,  $N_i$  is the number of frames for the *i*<sup>th</sup> trajectory, and  $MSD_i(n\Delta t)$  is the
- 674 individual MSD of the  $i^{\text{th}}$  trajectory for a time lag of  $n\Delta t$ .

#### 675 Estimation of the effective diffusion coefficient for the time scale of 1 s

- To calculate the effective diffusion coefficient,  $D_{eff}$ , a linear fit was made to the first 3 values to the ensemble MSD vs  $\tau$  plot (corresponding to  $\tau = 1/3$ , 2/3, and 1s). The slope of the fitted line was calculated to obtain MSD/ $\tau$ . The effective diffusion coefficient was calculated by  $D_{eff}$ =
- 679 MSD/(4  $\tau$ ).

#### 680 Particle size estimation

- 681 PEGylated particles were resuspended in an extract buffer without sucrose. The effective
- 682 diffusion coefficient for each type of particle was measured by particle tracking as above. The
- 683 diameters of the particles were calculated using a rearrangement of the Stokes-Einstein equation:
- 684  $d_{par} = k_B T / (3\pi \eta D_{eff})$ , where  $k_B$  is the Boltzmann constant (1.380649 · 10<sup>-23</sup> N m K<sup>-1</sup>), T is
- temperature (296.15 K), and  $\eta$  is the viscosity of extract buffer without sucrose (assumed to be
- 686 similar to water at 0.001 N m<sup>-2</sup> s).

29

### **Supplementary Information**

688

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Replica 1 Replica 2 FINT BSA (mg/mL) 0.8 1.7 3.1 6.3 12.5 25 50 100 146 228 1 138 241 2

690

## Figure S1. Trihalo compound-stained PAGE gel of proteins from 1x extract, filtrate, and 2x retentate

693 A representative trihalo compound-stained PAGE gel showing a BSA standard and two

694 biological replicates of extract, retentate, and filtrate. The estimated protein concentrations in

695 mg/mL (using the BSA standard as a reference) for the extract, retentate, and filtrate samples are

696 shown in orange. However, it should be noted that the trihalo compound used in staining the gel

697 depends on tryptophan residues to fluoresce. Since BSA has only 0.3% tryptophan residues

698 (compared to 1% in proteins overall), the protein concentrations in the extract, retentate, and

699 filtrate samples are likely overestimated. By Bradford assay the typical protein concentration of

700 extracts was 50-70 mg/mL.

31



Figure S2. Using nominal vs. measured protein concentrations to compare translation rates
 in different experiments.

(A) Translation rate as a function of nominal cytoplasmic concentration. These are the directlymeasured data from experiments where the eGFP mRNA concentration was kept constant and the translation machinery was proportional to the cytoplasmic concentration. Data points from same experiment are connected. Data are normalized relative to the translation rates at a cytoplasmic concentration of 1x. Relative cytoplasmic concentration are assumed to be 1.0 for 1x extract and 2.0 for the 2x retentate.

711 (B) Translation rate as a function of measured protein concentration. These are the directly-712 measured data from experiments where the eGFP mRNA concentration was kept constant and 713 the translation machinery was proportional to the cytoplasmic concentration. Data points from 714 same experiment are connected. Data are normalized relative to the translation rates at a 715 cytoplasmic concentration of 1x. Protein concentrations were measured for the starting extract 716 and the retentate, instead of assuming that they were 1x and 2x. Protein concentrations for the 717 dilutions were calculated from these the respective starting material. Note that the experiment-to-718 experiment variation is similar regardless of whether nominal or measured protein concentrations 719 are used.

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### Figure S3. Homeostasis in a Michaelis-Menten model of the effect of cytoplasmic concentration of translation and protein degradation.

- (A) Plot of Eq. S10, which relates a bimolecular reaction rate to the relative cytoplasmic
- 727 concentration, for various sizes of proteins, assuming that Michaelis-Menten kinetics are
- relevant. We assumed  $a = 0.018 \text{ nm}^{-1}$  (from Figure 4F) and arbitrarily chose the following values
- 729 for the parameters:  $E_{tot}[1] = S[1] = k_1[1] = k_{-1}[1] = k_2[1] = 1$ .
- 730 (B) Calculated optimal relative cytoplasmic concentration for proteins of different assumed sizes,
- assuming the same parameters.
- 732 (C) Fits of Eq. S10 to the experimental data.
- 733
- 734
- 735

33

# Movie S1. Effects of cytoplasmic concentration on self-organization and cycling in dilutions from 1x extract

- 738 SiR-tubulin staining (left) and SiR-tubulin fluorescence intensity as a function of time (right) in
- an extract after various dilutions. The same data are shown in Figure 1D. The starting material
- 740 was a 1x extract, diluted with various proportions of filtrate and imaged in a 96-well plate under
- 741 mineral oil. All fields are shown at equal exposure. The fluorescence intensities shown on the
- right were quantified from the center 1/9 of the wells and subsequently rescaled using the
- 743 maximum and minimum values to enhance the variability in the intensities, particularly in cases
- 744 of low cytoplasmic concentration.
- 745

# 746 Movie S2. Effects of cytoplasmic concentration on self-organization and cycling in dilutions 747 from 2x retentate

- 748 SiR-tubulin staining (left) and SiR-tubulin fluorescence intensity as a function of time (right) in
- an extract after various dilutions. The data were collected as in Movie S1 except that the starting
- 750 material was a 2x retentate. The same data are shown in Figure 1E.
- 751

### Movie S3. Cell-like compartment formation and cell cycle oscillation in 0.2x and 0.3x cytoplasm

SiR-tubulin staining was conducted on a 0.2x extract (left) and a 0.3x extract (right) as shown in

755 Movie S1 and Figure 1D. The fluorescence intensities were rescaled to improve the visibility of

the SiR-tubulin staining, and are displayed at a higher magnification,

34

#### 757 A model for the effect of diffusion on reaction rates assuming Michaelis-Menten kinetics

In the main text, we derived a simple model to account for the observed rates of protein

translation and degradation as a function of cytosolic protein concentration assuming a mass

action kinetics. Here, we assume a Michaelis-Menten enzymatic reaction kinetics to generate

response curves, and test if such an assumption also accounts the biphasic nature of the response

762 curves of protein translation and degradation vs cytoplasmic concentration.

To start, we assume that the rate determining reaction for each process is a biomolecularenzymatic reaction:

$$\mathsf{E} + \mathsf{S} \underset{k_{1}}{\overset{k_{1}}{\longleftrightarrow}} \mathsf{C} \overset{k_{2}}{\longrightarrow} \mathsf{E} + \mathsf{P}$$

765

where E is the enzyme, S the substrate, C the enzyme-substrate complex, and P the product of the reaction. If we assume that the system is in steady state, with  $\frac{dC}{dt} = 0$ , and that the substrate concentration is much higher than the enzyme concentration, then the rate of this process is described by the Michaelis-Menten equation:

770 
$$V = \frac{dP}{dt} = \frac{k_2 E_{tot} S}{\frac{k_- 1 + k_2}{k_1} + S},$$
 [Eq. S1]

771 where  $E_{tot} = E + C$ .

772 Next we want to add cytoplasmic concentration dependence to the terms on the right-hand side 773 of Eq. 2. The enzyme and substrate concentrations are linearly proportional to the relative 774 cytoplasmic concentration  $\phi$ . We can therefore write:

775 
$$E_{tot}[\phi] = \phi E_{tot}[1], \qquad [Eq. S2]$$

776 
$$S[\phi] = \phi S[1].$$
 .[Eq. S3]

777 Substituting into Eq. 2 yields:

778 
$$V = \frac{k_2 \phi^2 E_{tot}[1]S[1]}{\frac{k_{-1} + k_2}{k_1} + \phi S[1]}.$$
 [Eq. S4]

35

- Again, from the Smoluchowski equation (Smoluchowski, 1917) and Phillies's law (Eq. 1)
- 780 (Phillies, 1986; Phillies, 1988), we take the diffusion coefficients to be negative exponential
- 781 functions of the cytoplasmic protein concentration:

782 
$$k_1[\phi] \propto D_E[\phi] + D_S[\phi] = D_E[0]e^{-\mu_E\phi} + D_S[0]e^{-\mu_S\phi}.$$
 [Eq. S6]

For the special case where either one diffusion coefficient is much smaller than the other, or thescale factors are equal, we can simplify this to:

785 
$$k_1[\phi] = k_1[0]e^{-\mu\phi}$$
. [Eq. S7]

786 Similarly, we can rewrite Eq. S7 as:

787 
$$k_1[\phi] = k_1[1]e^{-\mu(\phi-1)}$$
. [Eq. S8]

We assume that  $k_{-1}$  varies with the diffusion coefficients and the cytoplasmic concentration in the same way, and that  $k_2$ , the rate constant for the catalytic step, is independent of the

790 cytoplasmic concentration. It follows that:

791 
$$V = \frac{k_2 \phi^2 E_{tot}[1]S[1]}{\frac{k_{-1}[1]e^{-\mu(\phi-1)} + k_2}{k_1[1]e^{-\mu(\phi-1)}} + \phi S[1]}.$$
 [Eq. S9]

Finally, since the scaling factor  $\mu$  is linearly proportional to the size of the diffusing particle  $d_p$ ,

793 we can write an expression that explicitly acknowledges particle size:

794 
$$V = \frac{k_2 \phi^2 E_{tot}[1]S[1]}{\frac{k_{-1}[1]e^{-ad_p(\phi-1)} + k_2}{k_1[1]e^{-ad_p(\phi-1)}} + \phi S[1]},$$
 [Eq. S10]

795 where a is a new scaling factor that relates  $d_p$  to  $\mu$ . Eq. S10 describes how the rate of a

796 Michaelis-Menten reaction whose reactants obey Phillies's law and the Smoluchowski equation

would be expected to vary with the cytoplasmic macromolecule concentration and moleculardiameter.

799

800

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| 803 | We do not have experimental estimates for most of the parameters in Eq. S10 (except for $a$ ,                     |
|-----|---|
| 804 | which, from Figure 4F is 0.018 nm <sup>-1</sup> ) for either translation or protein degradation. However, we      |
| 805 | can get a feel for Eq. S10 by arbitrarily assuming some parameter values $(E_{tot}[1] = S[1] =$                   |
| 806 | $k_1[1] = k_{-1}[1] = k_2[1] = 1$ ) and plotting <i>V</i> as a function of $\phi$ for macromolecules of different |
| 807 | assumed macromolecular diameters. The equation defines a biphasic, non-monotonic curve                            |
| 808 | (Figure S3A), and the larger the assumed macromolecular radius, the further to the left the                       |
| 809 | curve's maximum lies (Figure S3B). The observed rates for translation and degradation are fairly                  |
| 810 | well captured by assuming that the relevant macromolecules are 78 nm for translation and 0 nm                     |
| 811 | for degradation (Figure S3C).   |
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